

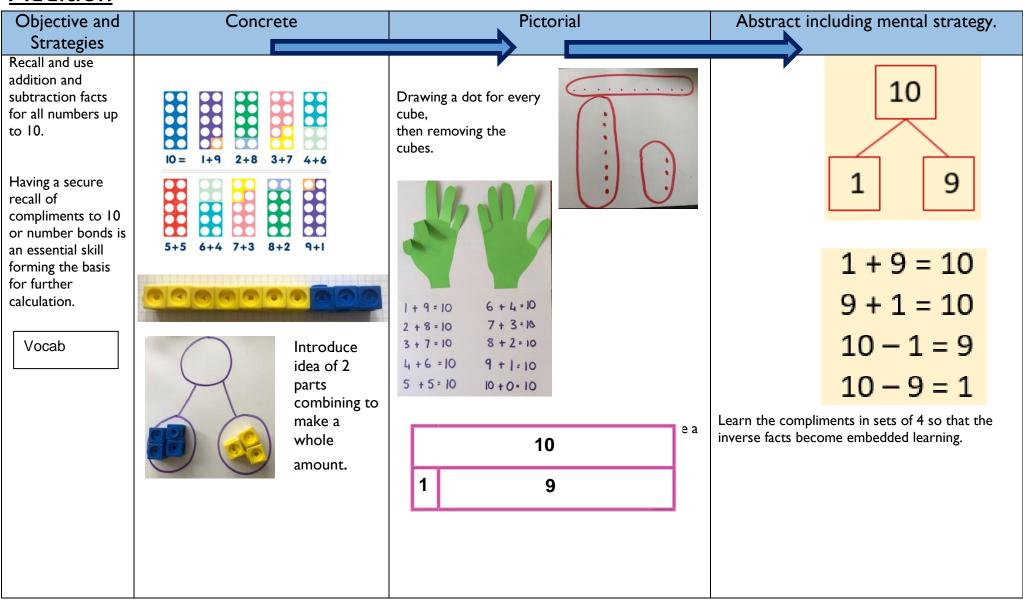
Mathematics Calculation Policy

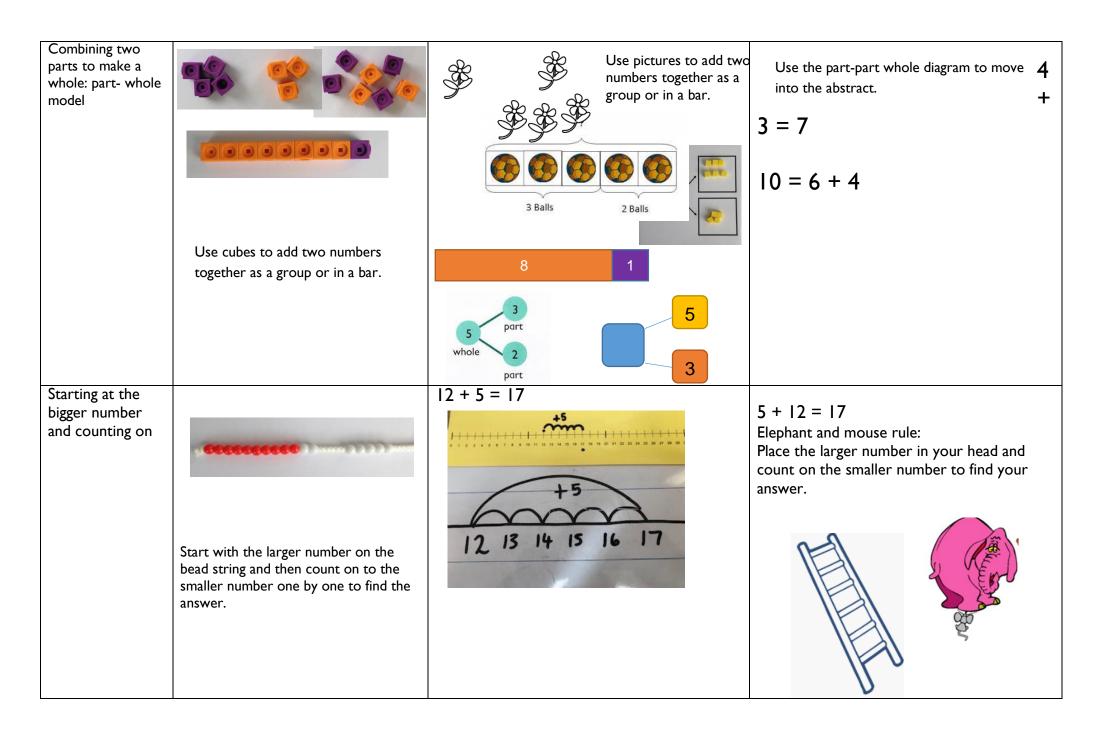
This policy is a statement of the aims, principles and strategies for teaching and learning of calculation strategies in Mathematics. At Elstow School we firmly believe in a mastery approach and use a schema from White Rose, who are leaders in the field of Mastery in Mathematics. This policy ensures that calculation is taught consistently across the school and that all staff are familiar with the most precise and effective delivery. The methods build understanding and confidence through learning in small steps, resulting in deeper mastery. This policy is also designed to help parents and carers support children's learning by providing an explanation of the methods used, in order for them to feel confident to assist in their children's learning.

The policy shows the progression of skills, knowledge and layout for written methods, set out in the following strands: addition & subtraction; multiplication & division. Early on, children are taught the inverse relationship between these.

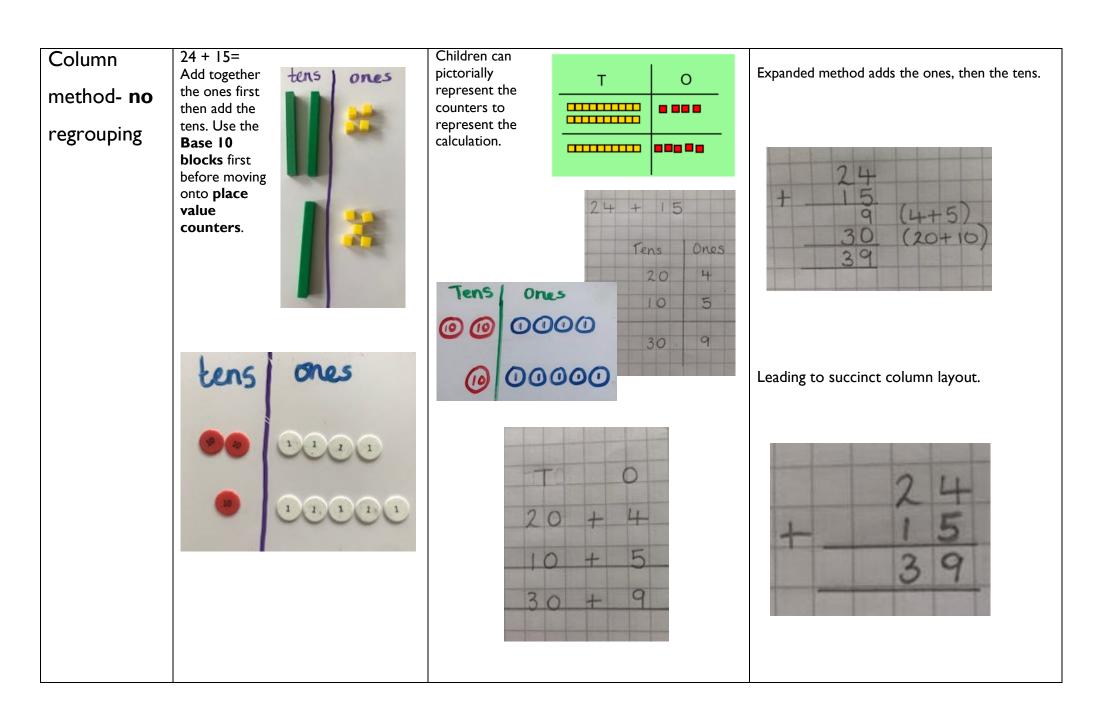
We follow a Concrete – Pictorial - Abstract model (CPA) which starts with a mathematical concept demonstrated through concrete resources (cubes, beads, counters) and then a pictorial representation (bar model, array) which echoes the concrete, used simultaneously with the concrete. This ensures a full understanding of the concept, before linking it to the abstract form (operation signs, equations). We recognise the importance of the use of correct and precise mathematical language and believe that all children are capable of learning mathematical terms. Mental calculation methods are complementary to written methods and should not be seen as separate from them. Children are taught how to mentally calculate efficiently and with accuracy. A demonstration of mastery is a reflection of child's ability to ascertain whether a calculation can be done mentally or requires a written method.

Addition





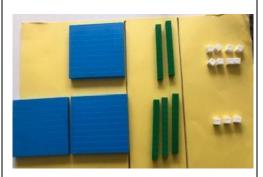
7 + 4= 11 Regrouping to If I am at seven, how many more do I need to make 10. make 10? How many more do I add on now? 6 + 5 = 11Use pictures or a number line. Regroup or Start with the partition the smaller number to make 10. larger number and use the smaller number to make 10. Adding three 4 + 7 + 6= 17 Put 4 and 6 together to make 10. Add single digits on 7. Combin e the two number s that make 10 and then add on the remaining number. Following on from making 10, make 10 Add together three groups of objects. with 2 of the digits (if possible) then add Draw a picture to recombine the groups on the third digit.



Column methodregrouping

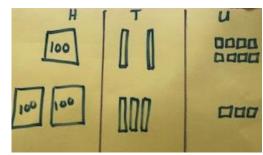
Make both numbers on a place value grid

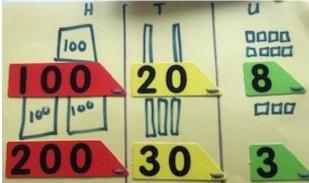
Introduce using Base 10, then move onto place value counters when the children are secure.



Children can draw a pictoral representation of the columns and place value counters.

Further support the understanding of plave value by using the arrow cards beneath the pictures.



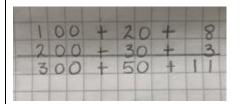


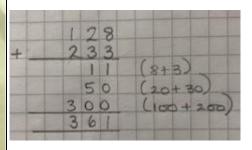
Then recombine to form the numbers.

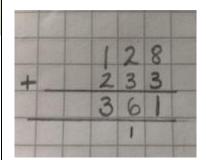


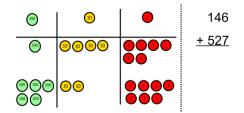
Start by partitioning the numbers before moving on to clearly show the exchange below the addition.

Start with a direct representation of the place value grid.

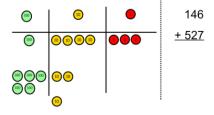








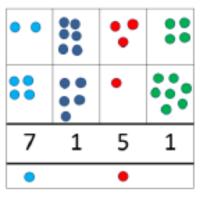
Add up the units and exchange 10 ones for one 10.



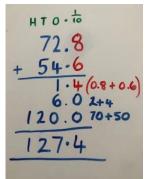
Add up the rest of the columns, exchanging the 10 counters from one column for the next place value column until every column has been added.

This can also be done with Base 10 to help children clearly see that 10 ones equal 1 ten and 10 tens equal 100.

As children move on to decimals, money and decimal place value counters can be used to support learning.

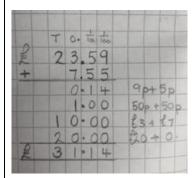


As the children move on, introduce decimals with the same number of decimal places and different, including money and measures.



Expanded method with tenths.

Expanded method with tenths and hundredths, such as money



When adding values with differing decimal places, pupils will add the place holding zeros to support the correct use of columns in succint additon methods.



Subtraction

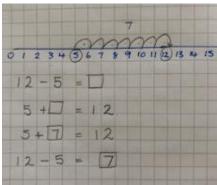
Objective and	Concrete	Pictorial	Abstract
Strategies			
Taking away ones	Use physical objects, such as counters and cubes to show how objects can be taken away. $6-2=4$	Cross out drawn objects to show what has been taken away.	8-2=6 $18-3=15$ $20=23-3$ $17- = 15$
Counting back	Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones. 13 – 4 Use counters and move them away from the group as you take them away counting backwards as you go.	Count back on a number line or number track 9 10 11 12 13 14 15 Start at the bigger number and count back the smaller number showing the jumps on the number line. -10 -10 -10 -10 -10 -10 -10 -10 -10 -1	Put 13 in your head, count back 4. What number are you at? Use your fingers to help. Don't count the number you are starting on as your first number.

Find the difference

Compare amounts and objects to find the difference.



Use number lines to count on to find the difference.



add to get to freeduy 10s

18 80

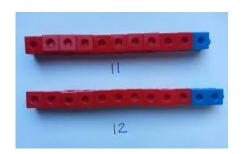
jump to friendly desert to 10s' number target number

10 + 6 + 2 = 18

add the jumps to find

the difference.

Use cubes to build towers or make bars to find the difference



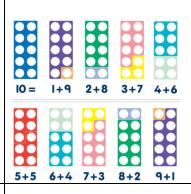
Which leads to **COMPARISON BAR MODELS**

Hannah has made 23 sandwiches, Helen made 15 sandwiches. How many more sandwiches did Hannah make?

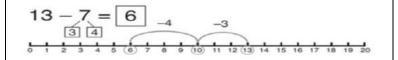
Use basic bar models with items to find the difference **Comparison Bar Models** 5 Pencils Lisa is 13 years old. Her sister is 22 years old. Find the difference in age between them. 13 Lisa 3 Erasers Sister 22 Draw bars to find the difference between 2 numbers. 23 15 Part- Whole Link to addition-Use a pictorial representation of objects to show the partuse the part whole model. 43 Model whole model to help explain the 100 inverse between addition and subtraction. Move to using numbers within If 10 is the whole the part whole model and 6 is one of the parts. What is the other alongside the abstract part? calculation. 100 - 43 = ?10 - 6 =

Make 10

Make 14 on the ten frame. Take away the four first to make 10 and then takeaway one more so you have taken away 5. You are left with the answer of 9.



Start at 13. Take away 3 to reach 10. Then take away the remaining 4 so you have taken away 7 altogether. You have reached your answer.

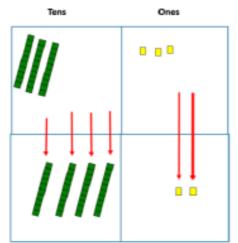


16 – 8=

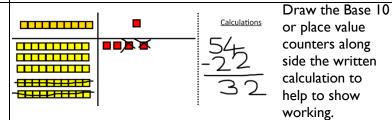
How many do we take off to reach the next 10?

How many do we have left to take off?

Column method without regrouping



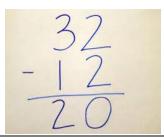
Use Base 10 to make the bigger number then take the smaller number away.

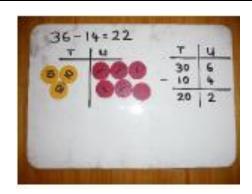


Calculations
176 - 64 =
176
- 64
112

47-24=23
40+7 _20+4
20+3

This will lead to a secure understadning of place value in written column subtraction.



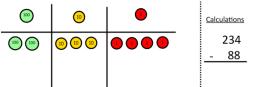


Show how you partition numbers to subtract. Again make the larger number first.

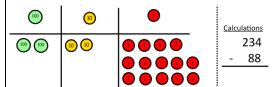
Column method with regrouping

Use Base 10 to start with before moving on to place value counters. Start with one exchange before moving onto subtractions with 2 exchanges.

Make the larger number with the place value counters

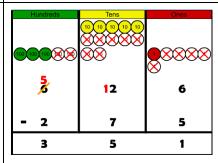


Start with the ones: can I take away 8 from 4 easily? I need to exchange one of my tens for ten ones.



Now I can subtract my ones.

Now look at the tens, can I take away 8

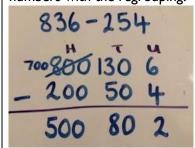


Draw the counters onto a place value grid and show what you have taken away by crossing the counters out as well as clearly showing the exchanges you make.

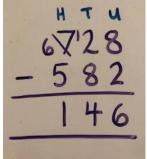
Just writing the numbers as shown here shows that the child understands the method and knows when to exchange/regroup.

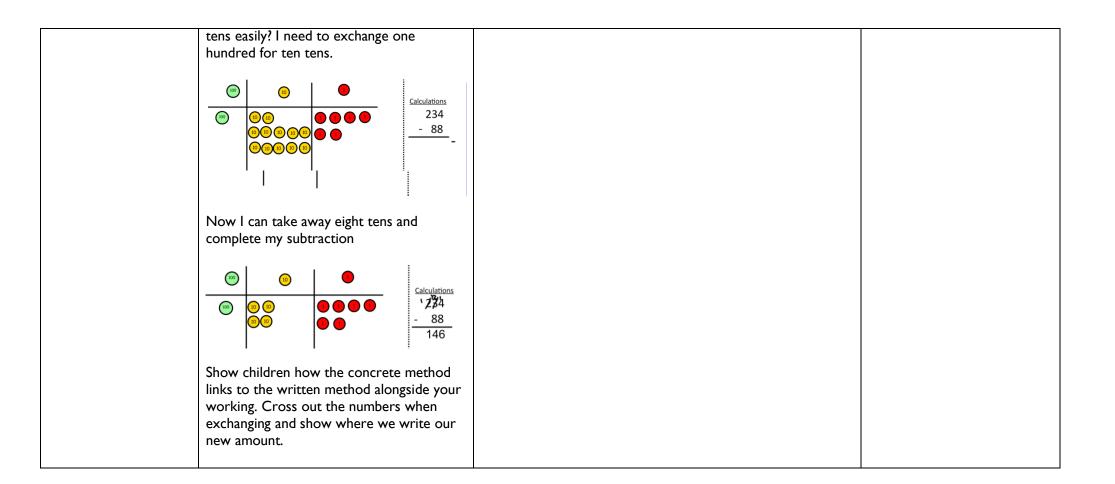
Moving forward the children use a more compact method.

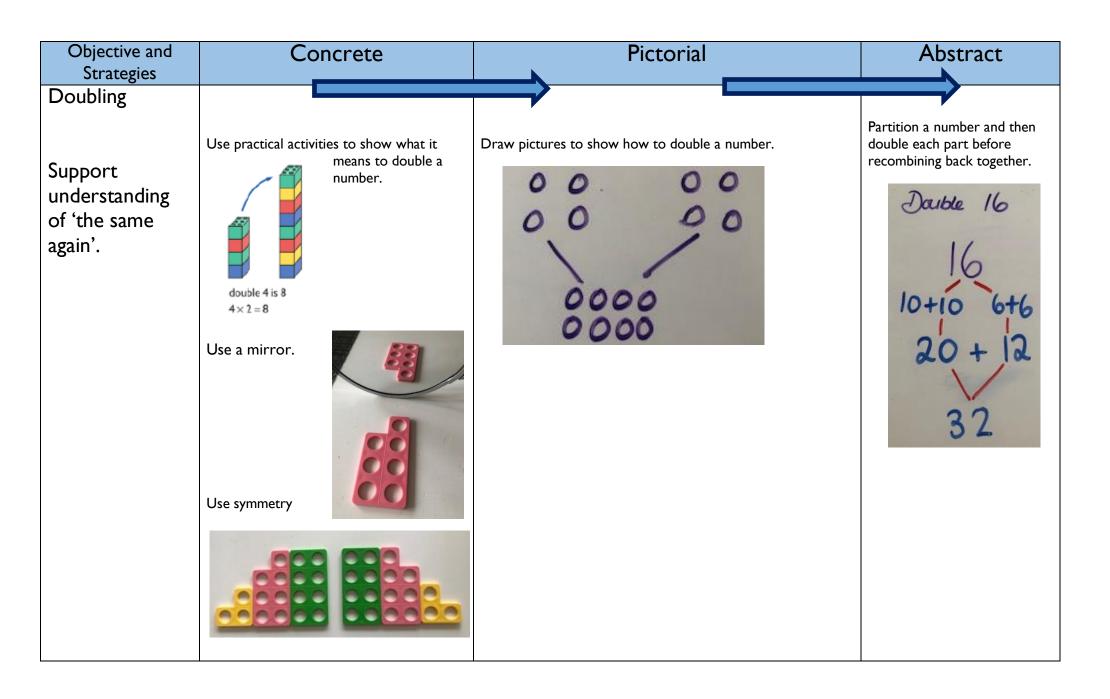
Children can start their formal written method by the number into clear place value columns. Show the partitioned numbers with the regrouping.



Three digits with regrouping a hunded into 10 tens.







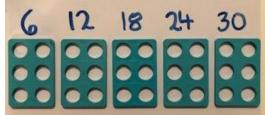
Counting in multiples

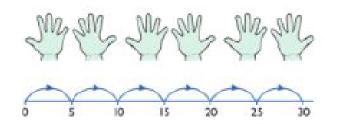


Count in multipl es support



ed by concrete objects in equal groups.





Use a number line or pictures to continue support in counting

Count in multiples of a number aloud.

Write sequences with multiples of numbers.

2, 4, 6, 8, 10

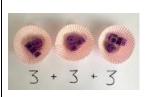
5, 10, 15, 20, 25, 30

Which of these numbers is not a multiple of 4?

40, 48, 56, 65 84

Repeated addition

It is fine to introduce the concept of 'multiples of a number' as repeated addition of that number, but this is only one way of looking at multiplication and only applies to positive whole numbers. Use different objects to add equal groups.



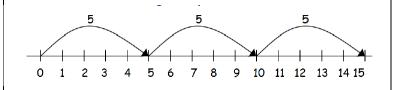


There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there?



in multiples.

2 add 2 add 2 equals 6



Write addition sentences to describe objects and pictures.



Arraysshowing commutative multiplication.

It is important use the correct terminology in multiplication, as part of rich mathematical knowledge.

Multiplicand- the number in our set.

Multiplier – the number of sets we have.

They multiply together to make a **product**.

Both multiplier and multiplicand are known as factors of that product.

Create arrays using counters, cubes and other to show multiplication sentences.

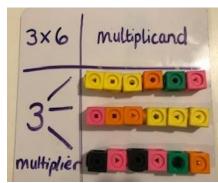




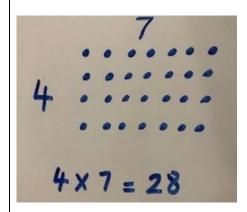
This array shows 3 lots of 5.



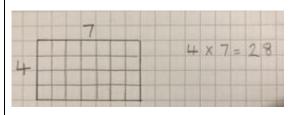
It is displayed here as 5 lots of 3



Draw arrays in different rotations to find **commutative** multiplication sentences.



Link arrays to area of rectangles.



Pupils should have plenty of experience of arrays to embedd understanding of how multiplication increases natural numbers rapidly, Use an array to write multiplication sentences and reinforce repeated addition.



$$5 + 5 + 5 = 15$$

 $3 + 3 + 3 + 3 + 3 = 15$

$$5 \times 3 = 15$$

Check understan $3 \times 5 = 15$ ding beyond learned facts with questioning.

What are the factors of 15?

Can 8 be a factor of 18? How do you know?

Finding factors

Being able to factorize a composite number into its component factors is an essential maths skill and leads into understanding of prime numbers.

How many different ways can you rearrange 12 cubes to form a rectangle?





3 X 4

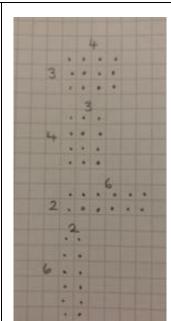




2 X 6

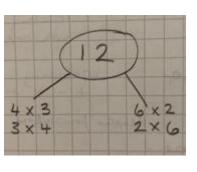


6 X 2

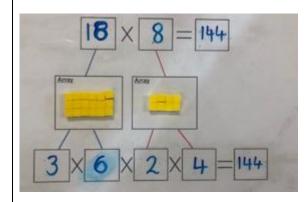


Draw the different arrays to show the factors.

List the factors in pairs.



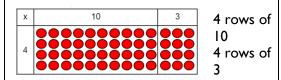
Once pupils are confident to find factors this can be applied to larger composite numbers



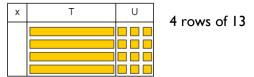
Grid Method

Misconceptions with place value can be avoided by using Base 10 and place value counters before numbers.

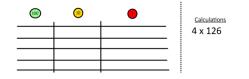
Show the link with arrays to first introduce the grid method.



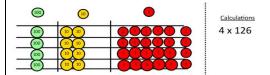
Move on to using Base 10 to move towards a more compact method.



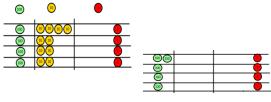
Move on to place value counters to show how we are finding groups of a number.We are multiplying by 4 so we need 4 rows.



Fill each row with 126.



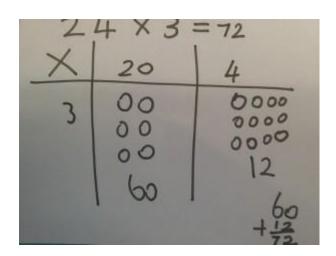
Add up each column, starting with the ones making any exchanges needed.



Then you have your answer.

Children can represent the work they have done with place value counters in a way that they understand.

They can draw the counters, using colours to show different amounts or just use circles in the different columns to show their thinking as shown below.

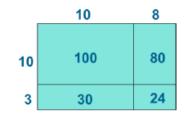


Start with multiplying by one digit numbers and showing the clear addition alongside the grid.

×	30	5
7	210	35

$$210 + 35 = 245$$

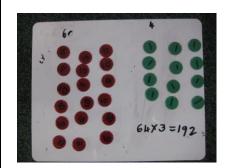
Moving forward, multiply by a 2 digit number showing the different rows within the grid method.



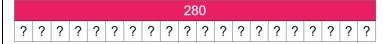
Х	1000	300	40	2
10	10000	3000	400	20
8	8000	2400	320	16

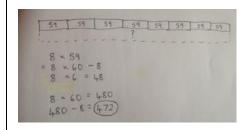
Column multiplication

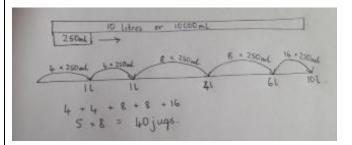
Children can continue to be supported by place value counters at the stage of multiplication.



It is important at this stage that they always multiply the ones first and note down their answer followed by the tens which they note below. Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written methods.







Start with long multiplication, reminding the children about lining up their numbers clearly in columns.

If it helps, children can write out what they are solving next to their answer.

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Division

Objective and Strategies	Concrete	Pictorial	Abstract
30, 4008,00			

Sharing objects into groups



I have 10 cubes, can you share them equally in 2 groups?





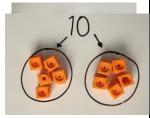
Children use pictures or shapes to share quantities.



people.

$$9 \div 3 = 3$$

Share 9 buns between three









Division as

grouping

Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.





$$96 \div 3 = 32$$

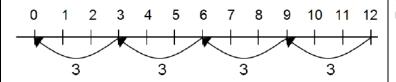




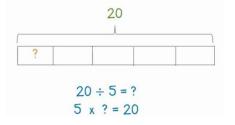




Use a number line to show jumps in groups. The number of jumps equals the number of groups.



Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group.

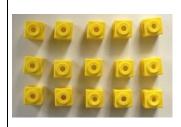




 $8 \div 2 = 4$

Divide 28 into 7 groups. How many are in each group?

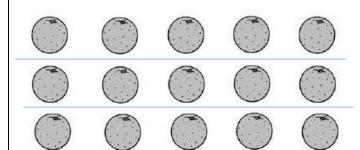
Division within arrays



Link division multiplication by creating an array and thinking about the number

sentences that can be created.

Eg $15 \div 3 = 5$	$5 \times 3 = 15$
$15 \div 5 = 3$	$3 \times 5 = 15$



Draw an array and use lines to split the array into groups to make multiplication and division sentences.

Find the inverse of multiplication and division sentences by creating four linking number sentences.

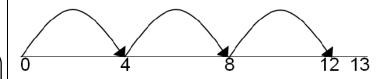
$$7 \times 4 = 28$$

 $4 \times 7 = 28$
 $28 \div 7 = 4$
 $28 \div 4 = 7$

Division with a remainder



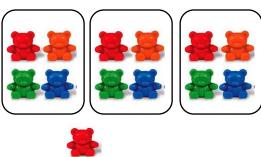
Divide objects between groups and see how much is left over



Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder.

Complete written divisions and show the remainder using





Draw dots and group them to divide an amount and clearly show a remainder.

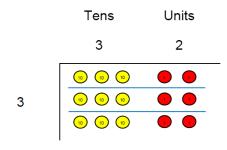






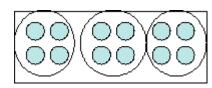


Short division



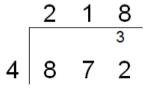
Use place value counters to divide using the bus stop method alongside

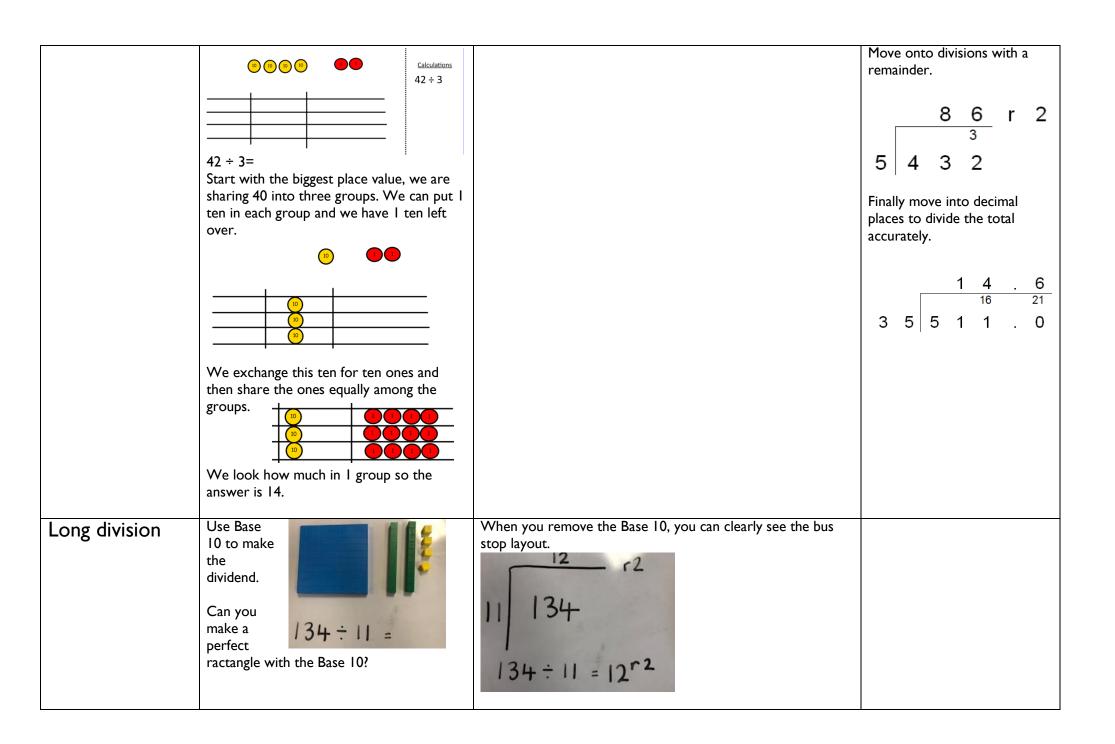
Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups.



Encourage them to move towards counting in multiples to divide more efficiently.

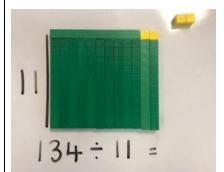
Begin with divisions that divide equally with no remainder.



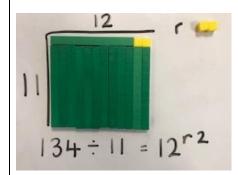




denominations for smaller ones.



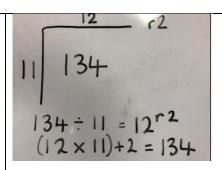
Lay the base 10 out in a rectangle with the divisor as the width. Draw in a line next to the divisor.



Count how many you have as the length of the rectangle.

Are there any left over that cannot form a a triangle?

This is your quotient and remainder.



Pupils then check using the inverse.

Always engourage pupils to write a WIK box (What I know) in multiples of the divisor to help before long division.

This helps them to estimate an answer and spot errors more easily.



